

# Ha Le

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## Education

- June 2003 • Ph.D. in Computer Science University of Waterloo, Canada  
**Thesis title:** Algorithms for the Construction of the Minimal Telescopers  
**Thesis co-supervisors:** Dr. K.O. Geddes, Dr. S.A. Abramov
- May 1999 • M.Math. in Computer Science University of Waterloo, Canada  
**Thesis title:** Client-Server Communication Standards for Mathematical Computation  
**Thesis supervisor:** Dr. G. Labahn
- May 1995 • Co-op Honours B.Math. in Computer Science University of Waterloo, Canada

## Research Interests

- Symbolic computation
- Computer graphics

## Employment

### *Research*

- Oct. 2004 – Present • Postdoctoral Fellowship Department of Mathematics,  
Simon Fraser University, Canada  
**Supervisor:** Dr. M. Monagan

Research in symbolic summation, and differential equations.

Software development in numerical analysis, and polynomial computation.

## Employment (continued)

- Sept. 2003 – Sept. 2004
- Postdoctoral Fellowship                      The French National Institute for  
Research in Computer Science and Control, France  
**Supervisor:** Dr. B. Salvy  
  
Research in symbolic summation and integration.  
  
Software development in series computation, and algorithms in  
skew-polynomial rings.
- Dec. 1996 – Apr. 2003
- Research Assistant                              Department of Computer Science,  
University of Waterloo, Canada  
**Supervisors:** Dr. K.O. Geddes, Dr. G. Labahn  
  
Designed and implemented algorithms in symbolic summation.  
  
Developed client-server communication standards for mathematical  
computation.  
  
Helped supervise co-op students.

### *Teaching*

- Jan. 2005 – Apr. 2005
- Instructor    Department of Mathematics, Simon Fraser University  
Taught a third-year course in computational numerical analysis  
<http://www.cecm.sfu.ca/~hle/teaching/MACM316/>.
- Dec. 1996 – Apr. 2003
- Teaching Assistant                              Department of Computer Science,  
University of Waterloo  
Acted as teaching assistant for courses in numerical analysis, soft-  
ware specification, and symbolic computation.

### *Industry*

- June 2003 – July 2003
- Consultant    Waterloo Maple Inc., Waterloo, Canada  
  
Designed and developed mathematical software.
- Sept. 1997 – Dec. 1997
- Consultant    Web Pearls Inc., Waterloo, Canada  
**Supervisor:** Dr. C.R. Howlett  
  
Developed client-server communication between computer algebra  
systems and the two international standards representing mathe-  
matical objects: OpenMath and MathML.

## Employment (continued)

- May 1994 – Nov. 1996 • Software developer Waterloo Maple Inc., Waterloo, Canada  
**Supervisor:** Dr. C.R. Howlett
- Designed and developed mathematical software which includes two packages in geometry, and the software which supports visualization of mathematical objects using Virtual Reality Modeling Language.
- Integrated software developed at various international research labs into the computer algebra system Maple. This included enforcing standards on coding, testing, and software documentation.
- Supervised co-op students.
- Jan. 1991 – Apr. 1994 • Co-op student and research assistant Symbolic  
 Computation Group, University of Waterloo, Canada  
**Supervisors:** Dr. K.O. Geddes, Dr. G. Labahn
- Involved in various development stages of Maple, including code development, testing, bug fixing. Designed and developed software in number theory, and visualization of mathematical objects.
- Sept. 1993 – Dec. 1993 • Co-op student Bell Northern Research, Ottawa, Canada
- Developed and maintained a simulation software package.

## List of Publications

### *Refereed Journal Publications*

- [1] • S.A. Abramov, H.Q. Le. On the order of the recurrence produced by the method of creative telescoping. *Discrete Mathematics*, 298, 2–17, Aug. 2005.
- [2] • S.A. Abramov, J.J. Carette, K.O. Geddes, H.Q. Le. Telescoping in the context of symbolic summation in Maple. *Journal of Symbolic Computation*, 38(4), 1303–1326, Oct. 2004.
- [3] • H.Q. Le. A direct algorithm to construct the minimal  $Z$ -pairs for rational functions. *Advances in Applied Mathematics* 30, 137–159, Feb. 2003.
- [4] • S.A. Abramov, H.Q. Le. A criterion for the applicability of Zeilberger’s algorithm to rational functions. *Discrete Mathematics*, 259, 1–17, Dec. 2002.
- [5] • H.Q. Le. On the  $q$ -analogue of Zeilberger’s algorithm to rational functions. *Programming and Comput. Software (Programmirovaniye)*, 27, 35–42, Jan-Feb 2001.

## List of Publications (continued)

- [6] • H.Q. Le. Mathematical graphical object representation. *Programming and Comput. Software (Programmirovanie)*, 26(6), 346–351 Nov-Dec 2000.
- [7] • H.Q. Le. Communication-oriented representation of mathematical objects. *Programming and Comput. Software (Programmirovanie)*, 26(1), 7–16, Jan-Feb 2000.

### *Refereed Conference Publications*

- [8] • K.O. Geddes, H.Q. Le, Z. Li. Differential rational normal forms and a reduction algorithm for hyperexponential functions. In J. Gutierrez, editor, *Proceedings of the 2004 International Symposium on Symbolic and Algebraic Computation*, 183–190, 2004.
- [9] • S.A. Abramov, H.Q. Le. Utilizing relationships among linear systems generated by Zeilberger’s algorithm. In *Proceedings of the 2004 Formal Power Series and Algebraic Combinatorics*, 29–38, 2004.
- [10] • S.A. Abramov, H.Q. Le, M. Petkovšek. Rational canonical forms and efficient representations of hypergeometric terms. In J.R. Sendra, editor, *Proceedings of the 2003 International Symposium on Symbolic and Algebraic Computation*, 7–14, 2003.
- [11] • S.A. Abramov, H.Q. Le. The sequence of linear algebraic systems generated by Zeilberger’s algorithm. *Proceedings of the 2003 Formal Power Series and Algebraic Combinatorics*, on CD 2003.
- [12] • H.Q. Le. Simplification of definite sums of rational functions by creative symmetrizing method. In T. Mora, editor, *Proceedings of the 2002 International Symposium on Symbolic and Algebraic Computation*, 161–167, 2002.
- [13] • S.A. Abramov, H.Q. Le. A lower bound for the order of telescopers for a hypergeometric term. In O. Foda, editor, *Proceedings of the 2002 Formal Power Series and Algebraic Combinatorics*, on CD, 2002.
- [14] • S.A. Abramov, K.O. Geddes, H.Q. Le. Computer algebra library for the construction of the minimal telescopers. In N. Takayama, A.M. Cohen and X. Gao, editors, *Proceedings of the 2002 International Congress of Mathematical Software*, 319–329, 2002.
- [15] • K.O. Geddes, H.Q. Le. An algorithm to compute the minimal telescopers for rational functions (differential – integral case). In N. Takayama, A.M. Cohen and X. Gao, editors, *Proceedings of the 2002 International Congress of Mathematical Software*, 453–463, 2002.
- [16] • H.Q. Le. A direct algorithm to construct Zeilberger’s recurrences for rational functions. In H. Barcelo and V. Welker, editors, *Proceedings of the 2001 Formal Power Series and Algebraic Combinatorics*, 303–312, 2001.

## List of Publications (continued)

- [17] • S.A. Abramov, H.Q. Le. Applicability of Zeilberger's algorithm to rational functions. In A.A. Mikhalev, D. Krob and A.V. Mikhalev, editors, *Proceedings of the 2000 Formal Power Series and Algebraic Combinatorics*, 91–102, 2000.
- [18] • H.Q. Le. On the differential-integral analogue of Zeilberger's algorithm to rational functions. In D. Wang and X. Gao, editors, *Proceedings of the 2000 Asian Symposium on Computer Mathematics*, 204–213, 2000.
- [19] • H.Q. Le, C.R. Howlett. Client-server communication standards for mathematical computation. In S. Dooley, editor, *Proceedings of the 1999 International Symposium on Symbolic and Algebraic Computation*, 299–306, 1999.

### *Technical Reports, Theses, Preprints*

- [20] • H.Q. Le, Z. Li. On a class of hyperexponential elements and the fast versions of Zeilberger's algorithm. KLMM research preprint, 23, Institute of Systems Sciences, AMSS, Academia Sinica, Dec. 2004.
- [21] • H.Q. Le. Algorithms for the construction of the minimal telescopers. PhD thesis, School of Computer Science, University of Waterloo, 2003.
- [22] • S.A. Abramov, H.Q. Le, Z. Li. OreTools: a computer algebra library for univariate Ore polynomial rings. Technical Report CS-2003-12, School of Computer Science, University of Waterloo, 2003.
- [23] • S.A. Abramov, K.O. Geddes, H.Q. Le. HypergeometricSum: a Maple package for finding closed forms of indefinite and definite sums of hypergeometric type. Technical Report CS-2001-24, School of Computer Science, University of Waterloo, 2001.
- [24] • S.A. Abramov, K.O. Geddes, H.Q. Le. A direct algorithm to construct the minimal telescopers for rational functions ( $q$ -difference case). Technical Report CS-2001-25, School of Computer Science, University of Waterloo, 2001.
- [25] • H.Q. Le. Computing the minimal telescoper for sums of hypergeometric terms. SIGSAM BULLETIN: *Communications on Computer Algebra*, 35(3):2–10, Sept. 2001.
- [26] • H.Q. Le. Client-server communication standards for mathematical computation. Master's thesis, School of Computer Science, University of Waterloo, 1999.

## Presentations

### *Invited Speaker*

- A report on Zeilberger's algorithm. Seminar in Symbolic Computation, Research Institute for Symbolic Computation (RISC), Linz, Austria, August 2004.
- Efficient representations of hypergeometric terms and the assignment problem. Seminar in Symbolic Computation, University of Limoges, France, November 2003.
- Algorithms and computer algebra library for the construction of the minimal telescopers. *Scientific Committee's Invitational Special Session of the 8th International Conference on Applications of Computer Algebra*, Volos, Greece, June 2002.
- LCLM techniques for constructing Zeilberger's recurrences. Seminar in Symbolic Computation, University of Limoges, France, October 2001.
- New features of Maple V Release 6. The Joint Institute of Nuclear Research, Dubna, Russia, July 1999.
- Some fun with MapleV Release 5. The Joint Institute of Nuclear Research, Dubna, Russia, September 1998.
- Communication-oriented representation of mathematical objects. *Monthly seminar on Computer Algebra*, Moscow States University, Moscow, Russia, October 1998.

### *Conference Papers*

- Differential rational normal forms and a reduction algorithm for hyperexponential functions. *The 2004 International Symposium on Symbolic and Algebraic Computation*, Santander, Spain, July 2004.
- Differential rational normal forms and representations of hyperexponential functions. The Ninth Rhine Workshop on Computer Algebra, University of Nijmegen, Nijmegen, The Netherlands, March 2004.
- Rational canonical forms and efficient representations of hypergeometric terms. *The 2003 International Symposium on Symbolic and Algebraic Computation*, Philadelphia, USA, August 2003.
- Computer algebra library for the construction of the minimal telescopers. *The 2002 International Congress of Mathematical Software*, Beijing, China, August 2002.
- An algorithm to compute the minimal telescopers for rational functions (differential – integral case). *The 2002 International Congress of Mathematical Software*, Beijing, China, August 2002.

## Presentations (continued)

- Simplification of definite sums of rational functions by creative symmetrizing method. *The 2002 International Symposium on Symbolic and Algebraic Computation*, Lille, France, July 2002.
- A direct algorithm to construct Zeilberger's recurrences for rational functions. *The 2001 Formal Power Series and Algebraic Combinatorics*, Arizona, USA, May 2001.
- On the differential-integral analogue of Zeilberger's algorithm to rational functions. *The 4th Asian Symposium on Computer Mathematics*, Chiang Mai, Thailand, December 2000.
- Applicability of Zeilberger's algorithm to rational functions. *The 2000 Formal Power Series and Algebraic Combinatorics*, Moscow, Russia, June 2000.
- Client-server communication standards for mathematical computation. *The 1999 International Symposium on Symbolic and Algebraic Computation*, Vancouver, Canada, July 1999.

## Awards and Scholarships

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|--------------------------|---|
| Fall 2001                | • Ontario Graduate Scholarship for Science and Technology.  |
| Spring 1992, Winter 1993 | • Natural Sciences and Engineering Research Council (NSERC) Undergraduate Student Research Award. |

## Professional Services

- Member of the Poster Committee of the 2005 International Symposium on Symbolic and Algebraic Computation, Beijing, China.
- Member of the Poster Committee of the 2004 International Symposium on Symbolic and Algebraic Computation, Cantabria, Santander, Spain.
- June 15, 2003 – July 8, 2003: visiting researcher at the Department of Computer Science & Cybernetics, Moscow State University, Moscow, Russia.
- Served as a referee for the Journal of Symbolic Computation, Advances in Applied Mathematics, 2004 and 2005 International Symposium on Symbolic and Algebraic Computation.
- Web Master, the 1999 International Symposium on Symbolic and Algebraic Computation.

## References

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